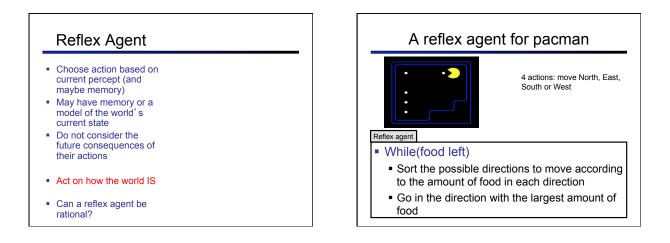
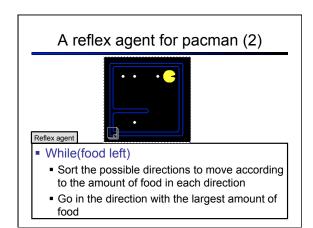
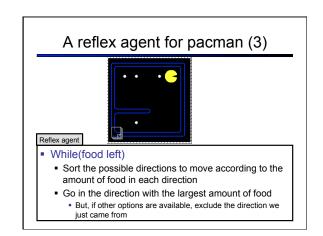


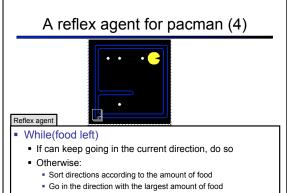
#### Reminder

- Only a very small fraction of AI is about making computers play games intelligently
- Recall: computer vision, natural language, robotics, machine learning, computational biology, etc.
- That being said: games tend to provide relatively simple example settings which are great to illustrate concepts and learn about algorithms which underlie many areas of AI

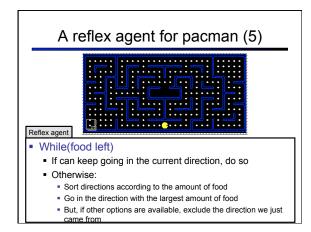


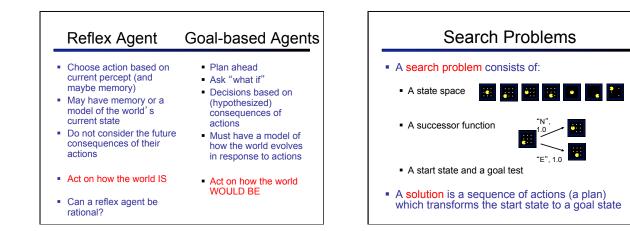


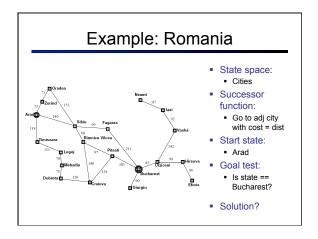


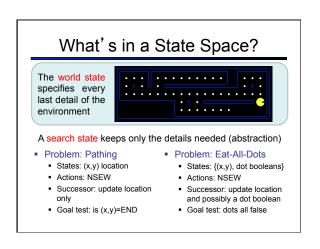


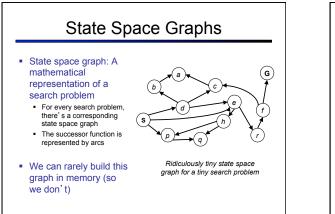
• But, if other options are available, exclude the direction we just

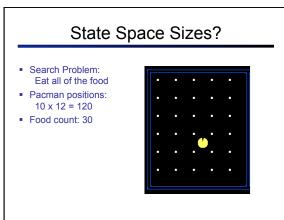


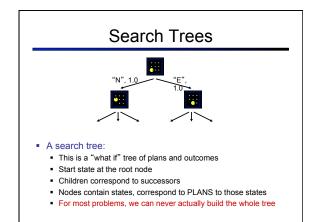


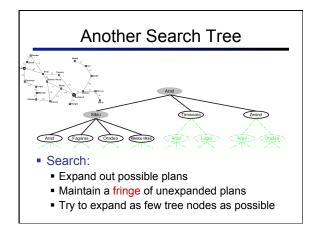


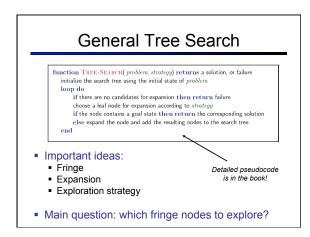


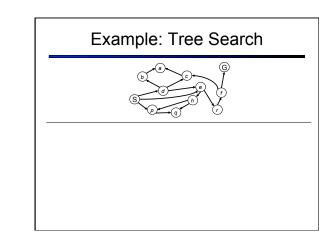


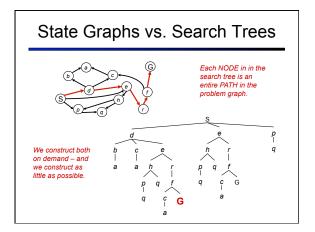


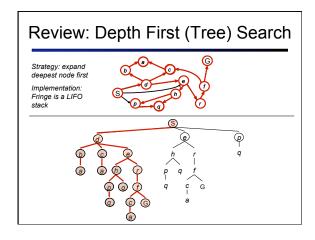


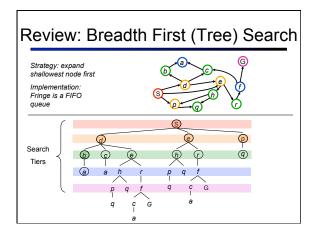


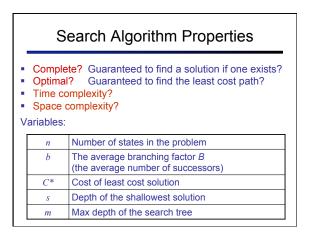


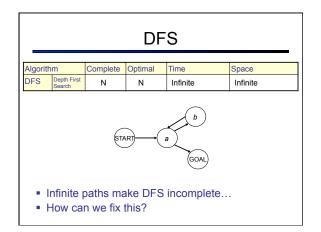


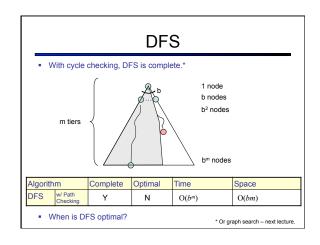




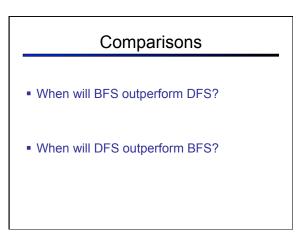


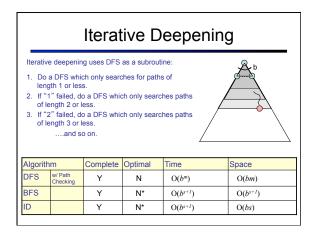


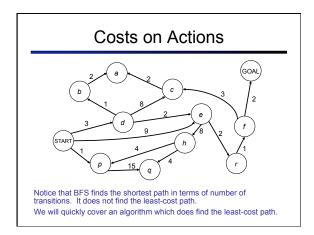


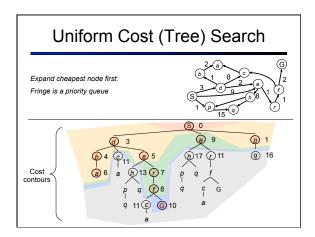


	BFS						
Algorit	hm	Complete	Optimal	Time	Space		
DFS	w/ Path Checking	Y	N	$O(b^m)$	O(bm)		
BFS		Y	N*	$O(b^{s+l})$	$O(b^{s+l})$		
	s tiers		A b	1 node b nodes b <sup>2</sup> nodes b <sup>s</sup> nodes			
	When is Bl	S optimal?	5	b <sup>m</sup> nodes			



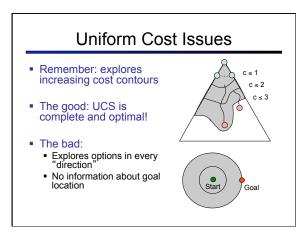


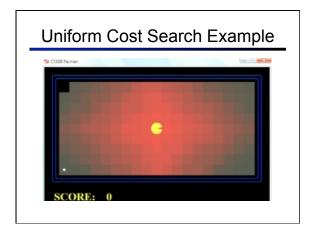


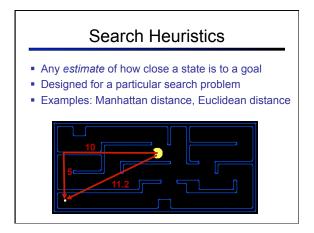


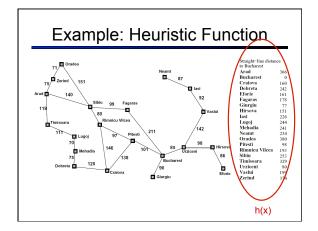
Prior	rity Queue Refresher
	a data structure in which you can insert and e) pairs with the following operations:
pq.push(key, value)	inserts (key, value) into the queue.
pq.pop()	returns the key with the lowest value, and removes it from the queue.
	a key's priority by pushing it again ueue, insertions aren't constant time,
<ul> <li>We'll need priority</li> </ul>	queues for cost-sensitive search methods

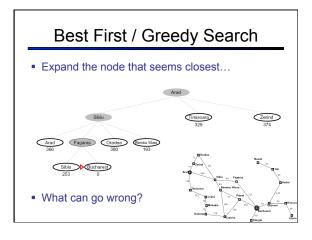
Algorit	:hm	Complete	Optimal	Time (in nodes)	Space
DFS	w/ Path Checking	Y	N	$O(b^m)$	O(bm)
BFS		Y	N	$O(b^{s+1})$	$O(b^{s+l})$
UCS		Y*	Y	$O(b^{C^{*/\epsilon}})$	$O(b^{C^{*/\epsilon}})$
	$C^*\!/\varepsilon$ tiers			ad	UCS can fail if ctions can get bitrarily cheap

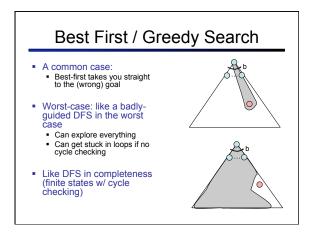


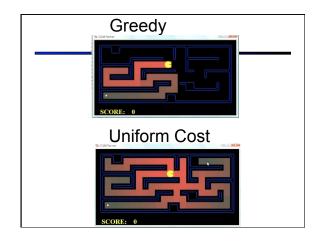


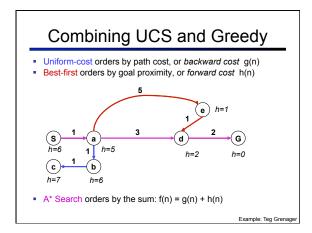


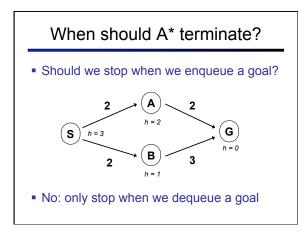


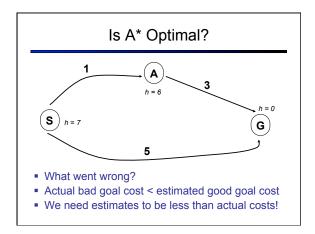


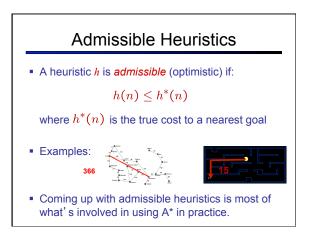


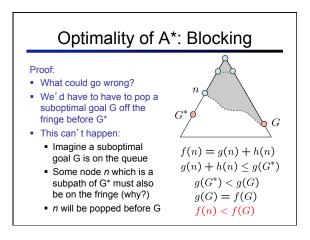


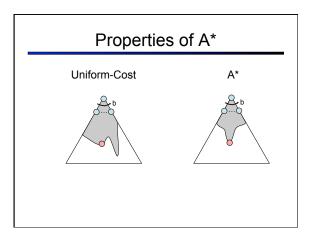


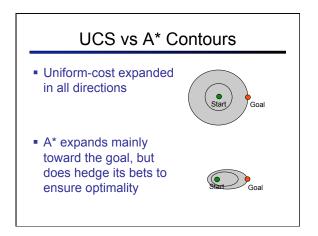


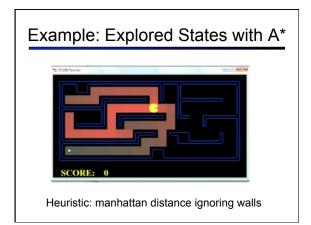


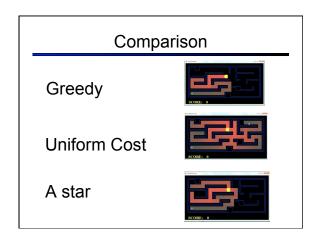


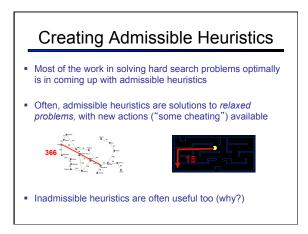


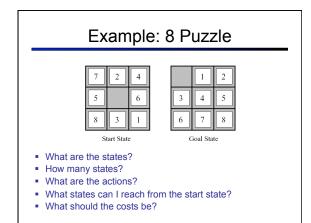


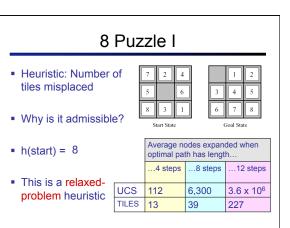


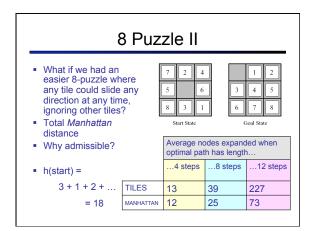


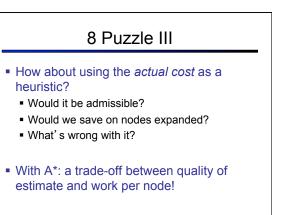


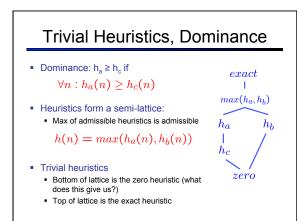


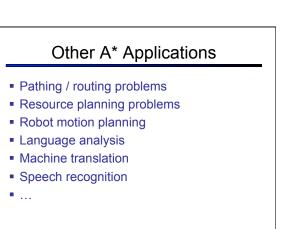


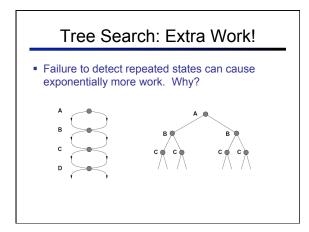


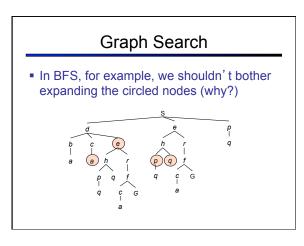






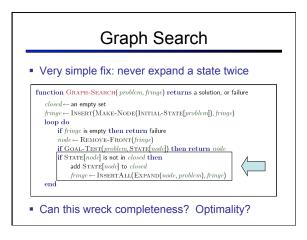


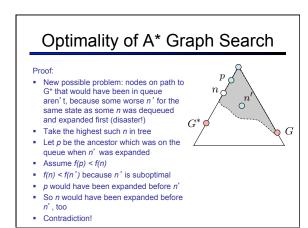


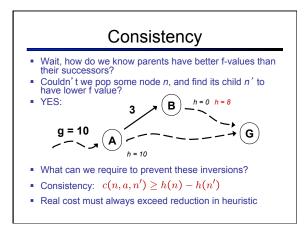


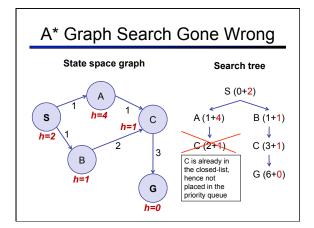
# Graph Search

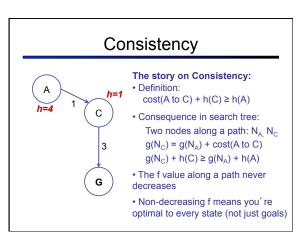
- Idea: never expand a state twice
- How to implement:
  - Tree search + list of expanded states (closed list)Expand the search tree node-by-node, but...
  - Before expanding a node, check to make sure its state is new
- Python trick: store the closed list as a set, not a list
- Can graph search wreck completeness? Why/why not?
- How about optimality?











#### **Optimality Summary**

- Tree search
- A\* optimal if heuristic is admissible (and non-negative) Uniform Cost Search is a special case (h = 0)
- Graph search: A\* optimal if heuristic is consistent
   UCS optimal (h = 0 is consistent)
- Consistency implies admissibility Challenge:Try to prove this. Hint: try to prove the equivalent statement not admissible implies not consistent
- In general, natural admissible heuristics tend to be consistent
- Remember, costs are always positive in search!

### Summary: A\*

- A\* uses both backward costs and (estimates of) forward costs
- A\* is optimal with admissible heuristics
- Heuristic design is key: often use relaxed problems

## A\* Memory Issues $\rightarrow$ IDA\*

- IDA\* (Iterative Deepening A\*)
  - 1. set f<sub>max</sub> = 1 (or some other small value)
  - 2. Execute DFS that does not expand states with f>fmax
  - 3. If DFS returns a path to the goal, return it
  - 4. Otherwise  $f_{max} = f_{max} + 1$  (or larger increment) and go to step 2
  - Complete and optimal
  - Memory: O(bs), where  $b \max$  branching factor, s searchdepth of optimal path
  - Complexity:  $O(kb^s)$ , where k is the number of times DFS is called

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## Recap Search I

- Agents that plan ahead  $\rightarrow$  formalization: Search
- Search problem:
  - States (configurations of the world)
  - Successor function: a function from states to
  - lists of (state, action, cost) triples; drawn as a graph
  - Start state and goal test
- Search tree:
  - Nodes: represent plans for reaching states
  - Plans have costs (sum of action costs)
- Search Algorithm:
- Systematically builds a search tree
- Chooses an ordering of the fringe (unexplored nodes)

### **Recap Search II**

• Tree Search vs. Graph Search

- Priority queue to store fringe: different priority functions → different search method
   Uninformed Search Methods

  - Uninformed Search Methods
     • Depth-First Search
     • Breadth-First Search
     • Uniform-Cost Search
     • Uniform-Cost Search
     • Leuristic Search Methods
     • Greedy Search
     • A\* Search heuristic design!
     • Search = heuristic design!
     • Consistency: (-n-y-) > h(h) = h(h). Furures when any note his expanded uning graph search the partial plants and ed in his the cheapest way to reach n.
     Time and space = complexity. completencess ontimality.
     • Complexity = complexity.
- Time and space complexity, completeness, optimality
- Iterative Deepening: enables to retain optimality with little computational overhead and better space complexity

